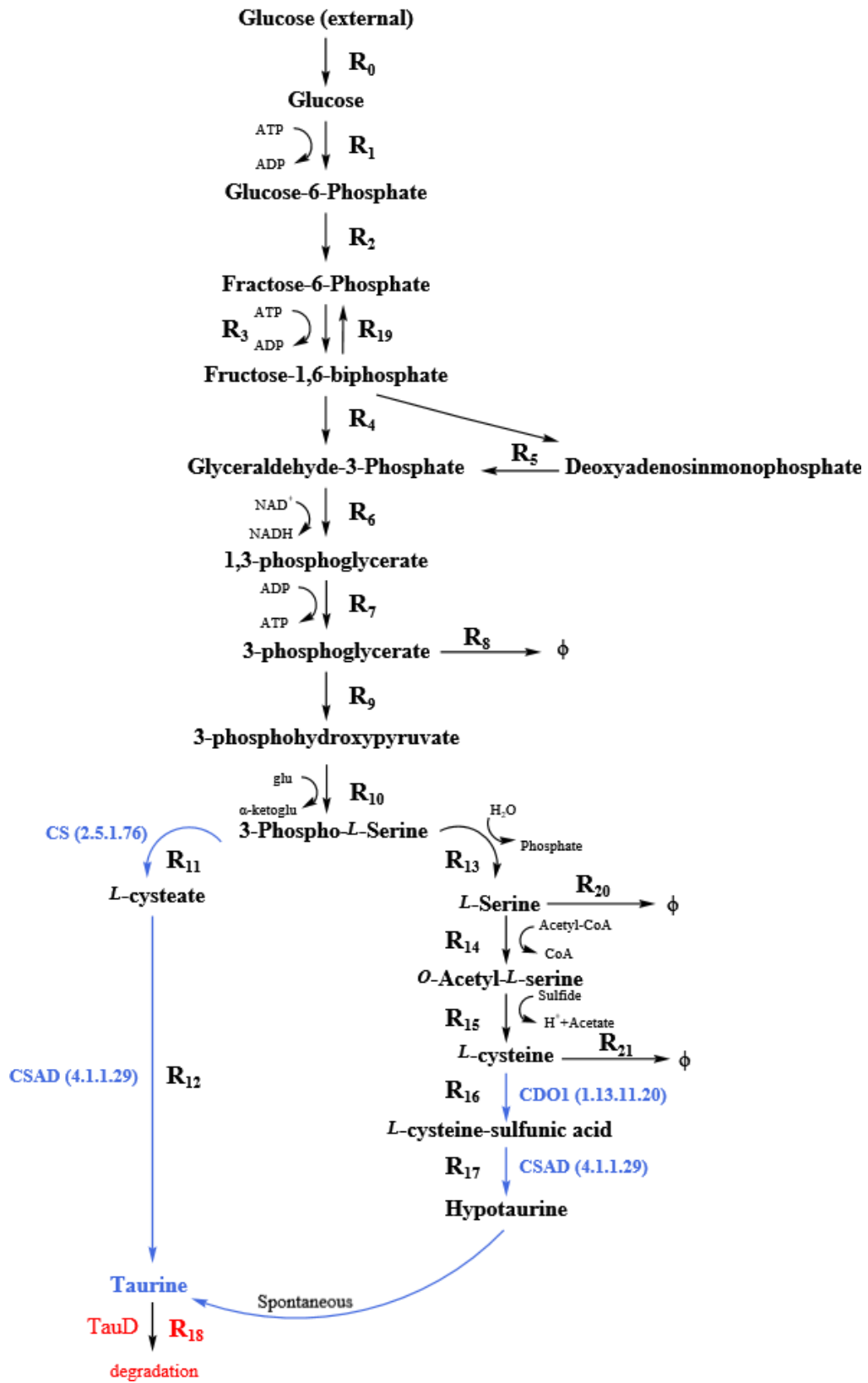


Supplementary Information of Model 1



Supplementary Table S1: Differential equations of the kinetic model

Equations

$$\frac{dC_{Glu}}{dt} = -r_1$$

$$\frac{dC_{G6P}}{dt} = r_1 - r_2$$

$$\frac{dC_{F6P}}{dt} = r_2 - r_3 + r_{19}$$

$$\frac{dC_{FBP}}{dt} = r_3 - r_{19} - r_4$$

$$\frac{dC_{DHAP}}{dt} = r_4 - r_5$$

$$\frac{dC_{GAP}}{dt} = r_4 + r_5 - r_6$$

$$\frac{dC_{PGP}}{dt} = r_6 - r_7$$

$$\frac{dC_{3PG}}{dt} = r_7 - r_8 - r_9$$

$$\frac{dC_{PHP}}{dt} = r_9 - r_{10}$$

$$\frac{dC_{PSer}}{dt} = r_{10} - r_{11} - r_{13}$$

$$\frac{dC_{Ser}}{dt} = r_{13} - r_{14} - r_{20}$$

$$\frac{dC_{OAS}}{dt} = r_{14} - r_{15}$$

$$\frac{dC_{Cys}}{dt} = r_{15} - r_{16} - r_{21}$$

$$\frac{dC_{Cystate}}{dt} = r_{11} - r_{12}$$

$$\frac{dC_{CSD}}{dt} = r_{16} - r_{17}$$

$$\frac{dC_{Taurine}}{dt} = r_{12} + r_{17} - r_{18} \text{ (optional)}$$

The C represents the concentration (mM) of each metabolite shown as subscript. The r represents the rate (mmol/mg/min) of each reaction shown as subscript.

Supplementary Table S2: Rate equations of the kinetic model

Reaction	Rate equation	Reference
PTS (R1)	$r_{PTS} = \frac{V_{\max_PTS} \cdot C_{GLC}^{extracellular} \cdot \frac{C_{PEP}}{C_{PYR}}}{\left(K_{m_PTS_a1} + K_{m_PTS_a2} \cdot \frac{C_{PEP}}{C_{PYR}} + K_{m_PTS_a3} \cdot C_{GLC}^{extracellular} + C_{GLC}^{extracellular} \cdot \frac{C_{PEP}}{C_{PYR}} \right) \cdot \left(1 + \frac{C_{G6P}^{n_{PTS}}}{K_{m_PTS_G6P}} \right)}$	1
PGI (R2)	$r_{PGI} = \frac{V_{\max_PGI} \cdot \left(C_{G6P} - \frac{C_{F6P}}{K_{eq_PGI}} \right)}{K_{m_PGI_G6P} \cdot \left(1 + \frac{C_{F6P}}{K_{m_PGI_F6P} \cdot \left(1 + \frac{C_{6PG}}{K_{m_PGI_F6P_6PGinh}} \right)} + \frac{C_{6PG}}{K_{m_PGI_G6P_6PGinh}} \right) + C_{G6P}}$	1
PFK (R3)	$r_{PFK} = \frac{V_{\max_PFK} \cdot C_{F6P}^{n_{PFK}} \cdot C_{ATP}}{\left(K_{m_PFK_F6P}^{n_{PFK}} + C_{F6P}^{n_{PFK}} \right) \cdot \left(K_{m_PFK_ATP} + C_{ATP} \right)}$	2
FBA (R4)	$r_{FBA} = \frac{V_{\max_FBA} \cdot \left(C_{FBP} - \frac{C_{GAP} \cdot C_{DHAP}}{K_{eq_FBA}} \right)}{K_{m_FBA_FBP} + C_{FBP} + \frac{K_{m_FBA_GAP} \cdot C_{DHAP}}{K_{eq_FBA} \cdot V_{blf}} + \frac{K_{m_FBA_DHAP} \cdot C_{GAP}}{K_{eq_FBA} \cdot V_{blf}} + \frac{C_{FBP} \cdot C_{GAP}}{K_{m_FBA_GAP_inh}} + \frac{C_{DHAP} \cdot C_{GAP}}{K_{eq_FBA} \cdot V_{blf}}}$	1,2

Supplementary Table S2: Continued

TPI (R5)	$r_{\text{TPI}} = \frac{V_{\text{max_TPI}} \cdot \left(C_{\text{DHAP}} - \frac{C_{\text{GAP}}}{K_{\text{eq_TPI}}} \right)}{K_{\text{m_TPI_DHAP}} \cdot \left(1 + \frac{C_{\text{GAP}}}{K_{\text{m_TPI_GAP}}} \right) + C_{\text{DHAP}}}$	1,2
GAPDH (R6)	$r_{\text{GAPDH}} = \frac{V_{\text{max_GAPDH}} \cdot \left(C_{\text{GAP}} \cdot C_{\text{NAD}} - \frac{C_{\text{PGP}} \cdot C_{\text{NADH}}}{K_{\text{eq_GAPDH}}} \right)}{\left(K_{\text{m_GAPDH_GAP}} \cdot \left(1 + \frac{C_{\text{PGP}}}{K_{\text{m_GAPDH_PGP}}} \right) + C_{\text{GAP}} \right) \cdot \left(K_{\text{m_GAPDH_NAD}} \cdot \left(1 + \frac{C_{\text{NADH}}}{K_{\text{m_GAPDH_NADH}}} \right) + C_{\text{NAD}} \right)}$	1,2
PGK (R7)	$r_{\text{PGK}} = \frac{V_{\text{max_PGK}} \cdot \left(C_{\text{ADP}} \cdot C_{\text{DGP}} - \frac{C_{\text{ATP}} \cdot C_{\text{3PG}}}{K_{\text{eq_PGK}}} \right)}{\left(K_{\text{m_PGK_ADP}} \cdot \left(1 + \frac{C_{\text{ATP}}}{K_{\text{m_PGK_ATP}}} \right) + C_{\text{ADP}} \right) \cdot \left(K_{\text{m_PGK_DGP}} \cdot \left(1 + \frac{C_{\text{3PG}}}{K_{\text{m_PGK_3PG}}} \right) + C_{\text{DGP}} \right)}$	1,2

Supplementary Table S2: Continued

Reaction	Rate equation and its parameters	Reference
PGDH (R9)	$r_{PGDH} = \frac{k_{cat_PGDH} \cdot E_{t_PGDH} \cdot \frac{C_{3PG}}{K_{m_PGDH_3PG}}}{\left(1 + \frac{C_{Ser}}{K_{i_PGDH_ser}}\right) \cdot \left(1 + \frac{C_{3PG}}{K_{m_PGDH_3PG}} + \frac{C_{PHP}}{K_{m_PGDH_PHP}}\right)}$	3
PSAT (R10)	$r_{PSAT} = \frac{k_{cat_PSAT} \cdot E_{t_PSAT} \cdot \frac{C_{PHP}}{K_{m_PSAT_PHP}}}{\left(1 + \frac{C_{PSEr}}{K_{m_PSAT_PSEr}} + \frac{C_{PHP}}{K_{m_PSAT_PHP}}\right)}$	3
CS (R11)	$r_{CS} = \frac{V_{max_CS} \cdot C_{PSEr}}{K_{m_CS_PSEr} + C_{PSEr}}$	M-M equation
CSAD_1 (R12)	$r_{CSAD_1} = \frac{V_{max_CSAD_1} \cdot C_{cystate}}{K_{m_CSAD_cystate} \cdot \left(1 + \frac{C_{CSA}}{K_{i_CSAD_CSA}}\right) + C_{cystate}}$	M-M equation

Supplementary Table S2: Continued

<p>PSP (R13)</p>	$r_{PSP} = \frac{k_{cat_PSP} \cdot E_{t_PSP} \cdot \frac{C_{Pser}}{K_{m_PSP_Pser}}}{\left(1 + \frac{C_{Pser}}{K_{m_PSP_Pser}} + \frac{C_{Ser}}{K_{m_PSP_Ser}}\right)}$	<p>3</p>
<p>SAT (R14)</p>	$r_{SAT} = \frac{V_{max_SAT} \cdot C_{Ser} \cdot C_{AcCoA}}{K_{m_SAT_AcCoA} \cdot C_{Ser} \cdot \left(1 + \frac{C_{Cys}}{K_{i_SAT_Cys1}}\right) + K_{m_SAT_Ser} \cdot C_{AcCoA} \cdot \left(1 + \frac{C_{Cys}}{K_{i_SAT_Cys2}}\right) + C_{Ser} \cdot C_{AcCoA}}$	<p>4</p>
<p>OASS (R15)</p>	$r_{OASS} = \frac{V_{max_OASS} \cdot C_{OAS}}{K_{m_OASS_OAS} \cdot \left(1 + \frac{C_{Cys}}{K_{i_OASS_Cys}} + \frac{K_{i_OASS_sulfide} \cdot C_{Cys}}{K_{i_OASS_Cys} \cdot C_{sulfide}}\right) + C_{OAS} \cdot \left(1 + \frac{K_{m_OASS_sulfide}}{C_{sulfide}}\right)}$	<p>4</p>
<p>CDO1 (R16)</p>	$r_{CDO1} = \frac{V_{max_CDO1} \cdot C_{Cys}}{K_{m_CDO1_Cys} + C_{Cys}}$	<p>M-M equation</p>
<p>CSAD_2 (R17)</p>	$r_{CSAD_2} = \frac{V_{max_CSAD_2} \cdot C_{CSA}}{K_{m_CSAD_CSA} \cdot \left(1 + \frac{C_{cystate}}{K_{i_CSAD_cystate}}\right) + C_{CSA}}$	<p>M-M equation</p>

Supplementary Table S2: Continued

Reaction	Rate equation and its parameters	Reference
FBPase (R19)	$r_{\text{FBPase}} = \frac{V_{\text{max_FBPase}} \cdot \frac{C_{\text{FBP}}}{K_{\text{m_FBPase_FBP}}} \cdot \left(1 + \frac{C_{\text{FBP}}}{K_{\text{m_FBPase_FBP}}}\right)^{n_{\text{FBPase}}-1}}{\left(1 + \frac{C_{\text{FBP}}}{K_{\text{m_FBPase_FBP}}}\right)^{n_{\text{FBPase}}} + \frac{L_{\text{FBPase}}}{\left(1 + \frac{C_{\text{PEP}}}{K_{\text{m_FBPase_PEP}}}\right)^{n_{\text{FBPase}}}}}$	2
Taurine Dioxygenase (R18)	$r_{\text{TauD}} = \frac{V_{\text{max_TauD}} \cdot C_{\text{Tau}}}{K_{\text{m_TauD}} + C_{\text{Tau}}}$	5
R8	$r_8 = 4 \cdot r_{\text{PGDH}}$	Estimate
R20	$r_{20} = \frac{1}{2} \cdot r_{\text{SAT}}$	Estimate
R21	$r_{21} = r_{\text{CDO1}}$	Estimate

Supplementary Table S3: Parameters of the Rate equations

Reaction	Equation	Parameter	Value	Unit	Source
PTS	Glu→G6P	$K_{m_PTS_a1}$	3082.3	mM	¹
		$K_{m_PTS_a2}$	0.01	mM	¹
		$K_{m_PTS_a3}$	245.3		¹
		$K_{m_PTS_G6P}$	2.15	mM	¹
		n_{PTS}	3.66	1	¹
		V_{max_PTS}	60000	mM /h	Estimated
		$C_{GLC}^{extracellular}$	optional	mM	
		C_{PEP}	2.67	mM	¹
		C_{PYR}	2.67	mM	¹
		C_{G6P}	0 / 3.48 *	mM	¹
PGI	G6P→F6P	K_{eq_PGI}	0.1725	1	¹
		$K_{m_PGI_G6P}$	2.9	mM	¹
		$K_{m_PGI_F6P}$	0.266	mM	¹
		$K_{m_PGI_F6P_6PGinh}$	0.2	mM	¹
		$K_{m_PGI_G6P_6PGinh}$	0.2	mM	¹
		V_{max_PGI}	8352	mM /h	⁶
		C_{G6P}	0 / 3.48 *	mM	¹
		C_{F6P}	0 / 0.60 *	mM	¹
		C_{6PG}	0.808	mM	¹
		PFK	F6P→FBP	$K_{m_PFK_F6P}$	0.13
$K_{m_PFK_ATP}$	0.12			mM	²
n_{PFK}	3.0			1	²
V_{max_PFK}	666			mM /h	⁶
C_{F6P}	0 / 0.60 *			mM	¹
C_{ATP}	4.27			mM	¹

*: initial concentration/ steady-state concentration in physiological state

Supplementary Table S3: Continued

Reaction	Equation	Parameter	Value	Unit	Source
FBA	FBP→GAP+DHAP	K_{eq_FBA}	0.144	1	1,2
		$K_{m_FBA_FBP}$	0.133	mM	1,2
		$K_{m_FBA_GAP}$	0.088	mM	1,2
		$K_{m_FBA_DHAP}$	0.088	mM	1,2
		$K_{m_FBA_GAP_inh}$	0.6	mM	1,2
		V_{blf}	2	1	1,2
		V_{max_FBA}	7728	mM/h	2
		C_{FBP}	0 / 0.272 *	mM	1
		C_{GAP}	0 / 0.218 *	mM	1
		C_{DHAP}	0 / 0.167 *	mM	1
TPI	DHAP→GAP	K_{eq_TPI}	1.39	1	1,2
		$K_{m_TPI_DHAP}$	2.8	mM	1,2
		$K_{m_TPI_GAP}$	0.3	mM	1,2
		V_{max_TPI}	1680	mM/h	6
		C_{DHAP}	0 / 0.167 *	mM	1
		C_{GAP}	0 / 0.218 *	mM	1
GAPDH	GAP→PGP	K_{eq_GAPDH}	0.63	1	1,2
		$K_{m_GAPDH_GAP}$	0.683	mM	1,2
		$K_{m_GAPDH_PGP}$	1.04	mM	1,2
			$\times 10^{-5}$		
		$K_{m_GAPDH_NAD}$	0.252	mM	1,2
		$K_{m_GAPDH_NADH}$	1.09	mM	1,2
		V_{max_GAPDH}	31212	mM/h	6
		C_{GAP}	0 / 0.218 *	mM	1
		C_{NAD}	1.47	mM	1
		C_{PGP}	0 / 0.008 *	mM	1
C_{NADH}	0.1	mM	1		

Supplementary Table S3: Continued

Reaction	Equation	Parameter	Value	Unit	Source
PGK	PGP→3PG	K_{eq_PGK}	1934.4	1	1,2
		$K_{m_PGK_ADP}$	0.185	mM	1,2
		$K_{m_PGK_ATP}$	0.653	mM	1,2
		$K_{m_PGK_DGP}$	0.0468	mM	1,2
		$K_{m_PGK_3PG}$	0.473	mM	1,2
		V_{max_PGK}	57960	mM/h	6
		C_{ADP}	0.595	mM	1
		C_{DGP}	0 / 0.008 *	mM	1
		C_{ATP}	4.27	mM	1
		C_{3PG}	0 / 2.13 *	mM	1
PGM	3PG→2PG	K_{eq_PGM}	0.188	1	1,2
		$K_{m_PGM_3PG}$	0.2	mM	1,2
		$K_{m_PGM_2PG}$	0.369	mM	1,2
		V_{max_PGM}	39600	mM/h	6
		C_{3PG}	0 / 2.13 *	mM	1
		C_{2PG}	0.399	mM	1
PGDH	3PG→PHP	k_{cat_PGDH}	1980	1/h	3
		E_t_PGDH	1.15	mM	3
		$K_{m_PGDH_3PG}$	1.2	mM	3
		$K_i_PGDH_Ser$	0.0038	mM	3
		$K_{m_PGDH_PHP}$	0.0032	mM	3
		C_{3PG}	0 / 2.13 *	mM	1
		C_{Ser}	0 / 4.9 *	mM	3
		C_{PHP}	0 / 0.6 *	mM	3
PSAT	PHP→PSer	k_{cat_PSAT}	6300	1/h	3
		E_t_PSAT	0.1	mM	3
		$K_{m_PSAT_PHP}$	0.0015	mM	3
		$K_{m_PSAT_PSEr}$	0.0017	mM	3
		C_{PHP}	0 / 0.6 *	mM	3
		C_{PSer}	0 / 0.09 *	mM	3
CS	PSer→cystate	$K_{m_CS_PSEr}$	6.2	mM	Estimated
		V_{max_CS}	6.144	mM/h	Estimated
		C_{PSer}	0 / 0.09 *	mM	3

Supplementary Table S3: Continued

Reaction	Equation	Parameter	Value	Unit	Source
CSAD_1	Cystate→Tau	$K_{m_CSAD_cystate}$	11.2	mM	Estimated
		$K_{i_CSAD_CSA}$	3.6	mM	Estimated
		$V_{max_CSAD_1}$	14.94	mM/h	Estimated
		$C_{cystate}$	0	mM	
		C_{CSA}	0	mM	
PSP	PSer→Ser	k_{cat_PSP}	5148	1/h	³
		E_{t_PSP}	0.25	mM	³
		$K_{m_PSP_PSer}$	0.0015	mM	³
		$K_{m_PSP_Ser}$	0.15	mM	³
		C_{PSer}	0 / 0.09 *	mM	³
		C_{Ser}	0 / 4.9 *	mM	³
SAT	Ser→OAS	$K_{m_SAT_AcCoA}$	0.58	mM	⁴
		$K_{i_SAT_Cys1}$	0.85	mM	⁴
		$K_{m_SAT_Ser}$	1.9	mM	⁴
		$K_{i_SAT_Cys2}$	1.5	mM	⁴
		V_{max_SAT}	72.2	mM/h	Estimated
		C_{Ser}	0 / 4.9 *	mM	³
		C_{AcCoA}	0.61	mM	⁷
		C_{Cys}	0 / 1.7 *	mM	Estimated
OASS	OAS→Cys	$K_{m_OASS_OAS}$	4.8	mM	⁴
		$K_{i_OASS_Cys}$	8.6	mM	⁴
		$K_{i_OASS_sulfide}$	0.011	mM	⁴
		$K_{m_OASS_sulfide}$	0.006	mM	⁴
		V_{max_OASS}	8660	mM/h	⁶
		C_{OAS}	0 / 7 *	mM	⁸
		C_{Cys}	0 / 1.7 *	mM	Estimated
		$C_{sulfide}$	0.005	mM	⁹
CDO1	Cys→CSD	$K_{m_CDO1_Cys}$	13.6	mM	Estimated
		V_{max_CDO1}	20.28	mM/h	Estimated
		V_{max_CDO1}	20.28	mM/h	Estimated
		C_{Cys}	0 / 1.7 *	mM	Estimated

Supplementary Table S3: Continued

Reaction	Equation	Parameter	Value	Unit	Source
CSAD_2	CSD→hypoTau	$K_{m_CSAD_CSA}$	3.6	<i>mM</i>	Estimated
		$K_{i_CSAD_cystate}$	11.2	<i>mM</i>	Estimated
		$V_{max_CSAD_2}$	30.42	<i>mM/h</i>	Estimated
		C_{CSA}	0	<i>mM</i>	
FBPase	FBP→F6P	$K_{m_FBPase_FBP}$	0.00892	<i>mM</i>	²
		n_{FBPase}	4	1	²
		L_{FBPase}	4000000	1	²
		$K_{m_FBPase_PEP}$	0.49	<i>mM</i>	²
		V_{max_FBPase}	777.6	<i>mM/h</i>	⁶
		C_{FBP}	0 / 0.272 *	<i>mM</i>	¹
		C_{PEP}	2.67	<i>mM</i>	¹
Taurine		V_{max_TauD}	2.61	<i>mM/h</i>	Estimated
Dioxygenase		K_{m_TauD}	0.058	<i>mM</i>	¹⁰

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