

# Resulting Temporal ODEs with the needed parameters

specific to pTet-circuit

$$(16) \Rightarrow \frac{d[FlhDC]}{dt} = b_{16}[pTet]_{eq} - \gamma_{35}[FlhDC] \quad (59a)$$

$$(35) \Rightarrow \frac{d[FlhDC]}{dt} = \beta_{16} \cdot \frac{K_{13}^{n_{13}}}{K_{13}^{n_{13}} + \left( \frac{K_{12}^{n_{aTc}}}{K_{12}^{n_{aTc}} + [aTc]_i^{n_{aTc}}} \cdot [TetR] \right)^{n_{13}}} - \gamma_{35}[FlhDC] \quad (59)$$


---

specific to pFlhDC-circuit

$$(17) \Rightarrow \frac{d[FlhDC]}{dt} = b_{17}[pFlhDC^{free}]_{eq} + b_{22}[(FliA)_{n_6} \blacktriangleright pFlhDC]_{eq} - \gamma_{35}[FlhDC] \quad (60a)$$

$$(22) \Rightarrow \frac{d[FlhDC]}{dt} = b_{17}[pFlhDC^{free}]_{eq} + b_{22}[(FliA)_{n_6} \blacktriangleright pFlhDC]_{eq} - \gamma_{35}[FlhDC]$$

$$(35) \Rightarrow \frac{d[FlhDC]}{dt} = \frac{K_{15}^{n_{15}}}{K_{15}^{n_{15}} + [OmpR^*]^{n_{15}}} \left( \beta_{17} \cdot \frac{K_6^{n_6}}{K_6^{n_6} + [FliA]^{n_6}} + \beta_{22} \cdot \frac{[FliA]^{n_6}}{K_6^{n_6} + [FliA]^{n_6}} \right) - \gamma_{35}[FlhDC] \quad (60)$$


---

$$(18) \Rightarrow \frac{d[FliA]}{dt} = b_{18}[(FlhDC)_{n_1} \blacktriangleright pFliA]_{eq} + b_{23}[(FliA)_{n_7} \blacktriangleright pFliA]_{eq} - \gamma_{36}[FliA] \quad (61a)$$

$$(23) \Rightarrow \frac{d[FliA]}{dt} = b_{18}[(FlhDC)_{n_1} \blacktriangleright pFliA]_{eq} + b_{23}[(FliA)_{n_7} \blacktriangleright pFliA]_{eq} - \gamma_{36}[FliA]$$

$$(36) \Rightarrow \frac{d[FliA]}{dt} = \beta_{18} \cdot \frac{[FlhDC]^{n_1}}{K_1^{n_1} + [FlhDC]^{n_1}} + \beta_{23} \cdot \frac{[FliA]^{n_7}}{K_7^{n_7} + [FliA]^{n_7}} - \gamma_{36}[FliA] \quad (61)$$


---

$$(24) \Rightarrow \frac{d[FP1]}{dt} = b_{24}[(FlhDC)_{n_2} \blacktriangleright pFliL]_{eq} + b_{25}[(FliA)_{n_8} \blacktriangleright pFliL]_{eq} - \gamma_{37}[FP1] \quad (62a)$$

$$(25) \Rightarrow \frac{d[FP1]}{dt} = b_{24}[(FlhDC)_{n_2} \blacktriangleright pFliL]_{eq} + b_{25}[(FliA)_{n_8} \blacktriangleright pFliL]_{eq} - \gamma_{37}[FP1]$$

$$(37) \Rightarrow \frac{d[FP1]}{dt} = \beta_{24} \cdot \frac{[FlhDC]^{n_2}}{K_2^{n_2} + [FlhDC]^{n_2}} + \beta_{25} \cdot \frac{[FliA]^{n_8}}{K_8^{n_8} + [FliA]^{n_8}} - \gamma_{37}[FP1] \quad (62)$$


---

specific to pFlagA-circuit

$$(26) \Rightarrow \frac{d[FP2]}{dt} = b_{26}[(FlhDC)_{n_3} \blacktriangleright pFlagA]_{eq} + b_{27}[(FliA)_{n_9} \blacktriangleright pFlagA]_{eq} - \gamma_{38}[FP2] \quad (63a)$$

$$(27) \Rightarrow \frac{d[FP2]}{dt} = b_{26}[(FlhDC)_{n_3} \blacktriangleright pFlagA]_{eq} + b_{27}[(FliA)_{n_9} \blacktriangleright pFlagA]_{eq} - \gamma_{38}[FP2]$$

$$(38) \Rightarrow \frac{d[FP2]}{dt} = b_{26}[(FlhDC)_{n_3} \blacktriangleright pFlagA]_{eq} + b_{27}[(FliA)_{n_9} \blacktriangleright pFlagA]_{eq} - \gamma_{38}[FP2]$$

$$(48) \Rightarrow \frac{d[FP2]}{dt} = \beta_{26} \cdot \frac{[FlhDC]^{n_3}}{K_3^{n_3} + [FlhDC]^{n_3}} + \beta_{27} \cdot \frac{[FliA]^{n_9}}{K_9^{n_9} + [FliA]^{n_9}} - \gamma_{38}[FP2] \quad (63)$$

$$\begin{aligned} (28) \\ (29) \Rightarrow \frac{d[FP2]}{dt} &= b_{28}[(FlhDC)_{n_4} \blacktriangleright pFlgB]_{eq} + b_{29}[(FliA)_{n_{10}} \blacktriangleright pFlgB]_{eq} - \gamma_{38}[FP2] \\ (38) \end{aligned} \quad (64a)$$

$$(50) \Rightarrow \frac{d[FP2]}{dt} = \beta_{28} \cdot \frac{[FlhDC]^{n_4}}{K_4^{n_4} + [FlhDC]^{n_4}} + \beta_{29} \cdot \frac{[FliA]^{n_{10}}}{K_{10}^{n_{10}} + [FliA]^{n_{10}}} - \gamma_{38}[FP2] \quad (64)$$

$$\begin{aligned} (30) \\ (31) \Rightarrow \frac{d[FP3]}{dt} &= b_{30}[(FlhDC)_{n_5} \blacktriangleright pFlhB]_{eq} + b_{31}[(FliA)_{n_{11}} \blacktriangleright pFlhB]_{eq} - \gamma_{39}[FP3] \\ (39) \end{aligned} \quad (65a)$$

$$(52) \Rightarrow \frac{d[FP3]}{dt} = \beta_{30} \cdot \frac{[FlhDC]^{n_5}}{K_5^{n_5} + [FlhDC]^{n_5}} + \beta_{31} \cdot \frac{[FliA]^{n_{11}}}{K_{11}^{n_{11}} + [FliA]^{n_{11}}} - \gamma_{39}[FP3] \quad (65)$$

specific to pTet-circuit

$$\begin{aligned} (19) \\ (32) \Rightarrow \frac{d[TetR]}{dt} &= b_{30}[(FlhDC)_{n_5} \blacktriangleright pFlhB]_{eq} + b_{31}[(FliA)_{n_{11}} \blacktriangleright pFlhB]_{eq} - \gamma_{40}[TetR] \\ (40) \end{aligned} \quad (66a)$$

$$(52) \Rightarrow \frac{d[TetR]}{dt} = \beta_{30} \cdot \frac{[FlhDC]^{n_5}}{K_5^{n_5} + [FlhDC]^{n_5}} + \beta_{31} \cdot \frac{[FliA]^{n_{11}}}{K_{11}^{n_{11}} + [FliA]^{n_{11}}} - \gamma_{40}[TetR] \quad (66)$$

*eqn.(55) gives then  $[TetR^{free}]$  in function of  $[TetR^{total}] := [TetR]$*

specific to pFlhDC/EnvZ-circuit

$$\begin{aligned} (21) \\ (34) \Rightarrow \frac{d[EnvZ]}{dt} &= b_{30}[(FlhDC)_{n_5} \blacktriangleright pFlhB]_{eq} + b_{31}[(FliA)_{n_{11}} \blacktriangleright pFlhB]_{eq} - \gamma_{42}[EnvZ] \\ (42) \end{aligned} \quad (67a)$$

$$(52) \Rightarrow \frac{d[EnvZ]}{dt} = \beta_{30} \cdot \frac{[FlhDC]^{n_5}}{K_5^{n_5} + [FlhDC]^{n_5}} + \beta_{31} \cdot \frac{[FliA]^{n_{11}}}{K_{11}^{n_{11}} + [FliA]^{n_{11}}} - \gamma_{42}[EnvZ]$$

$$(53) \qquad \qquad \qquad (67b)$$

$$[EnvZ^{total}] = [EnvZ_b] + [EnvZ] \qquad \qquad \qquad (67)$$

Solve then eqn.(57) to get  $[OmpR^*]$  in function of  $[OmpR^{total}] := [OmpR_b]$

specific to pFlhDC/OmpR\*-circuit

$$(20) \qquad \qquad \qquad (68a)$$

$$(33) \Rightarrow \frac{d[OmpR^*]}{dt} = b_{30}[(FlhDC)_{n_5} \blacktriangleright pFlhB]_{eq} + b_{31}[(FliA)_{n_{11}} \blacktriangleright pFlhB]_{eq} - \gamma_{43}[OmpR^*]$$

$$(43) \qquad \qquad \qquad (68a)$$

$$(52) \Rightarrow \frac{d[OmpR^*]}{dt} = \beta_{30} \cdot \frac{[FlhDC]^{n_5}}{K_5^{n_5} + [FlhDC]^{n_5}} + \beta_{31} \cdot \frac{[FliA]^{n_{11}}}{K_{11}^{n_{11}} + [FliA]^{n_{11}}} - \gamma_{43}[OmpR^*]$$

$$(53) \qquad \qquad \qquad (68)$$